

# Abstract Machines

*Summer Semester 2005*

3. Homework

Deadline: 6 May 2005 12:00

## Exercise 1:

6 Points

Write the following functions in OCaml (without using OCaml library functions with the same names).

- filter*, which takes as argument a predicate  $p$  and a list  $l$ , and returns the list of elements from  $l$  for which  $p$  is true.
- fold\_right*, such that
$$\text{fold\_right } f \ e \ [x_1, \dots, x_n] = f(x_1, f(x_2, \dots, f(x_n, e)) \dots).$$
- mapi*, such that
$$\text{mapi } f \ [x_1, \dots, x_n] = [f(x_1, 1), \dots, f(x_n, n)].$$
For example, for  $f(x, i) = x + i$  and  $l = [3, 3, 3]$ , *mapi*  $f$   $l$  should return  $[4, 5, 6]$ .

## Exercise 2:

4+4 Points

- Give a formal definition of the function *free* such that  $\text{free}(e) \subseteq \text{Vars}$  is the set of global variables in  $e$ .
- Determine the set of global variables for each of the following expressions.
  - $(\text{fn } x \Rightarrow x \ y) \ (\text{fn } y \Rightarrow y)$
  - $\text{fn } x, y \Rightarrow z \ (\text{fn } z \Rightarrow z \ (\text{fn } x \Rightarrow y))$
  - $(\text{fn } x, y \Rightarrow x \ z \ (y \ z)) \ (\text{fn } x \Rightarrow y \ (\text{fn } y \Rightarrow y))$
  - $((\text{fn } x \Rightarrow x) \ z) + \text{let } a = x; \\ \quad \quad \quad x = f \ y; \\ \quad \quad \quad y = z \\ \text{in } x+y+z$

## Exercise 3:

6 Points

Consider the expression  $e \equiv \text{if } x > 1 \text{ then } x \text{ else } x + y * x$  along with the address environment  $\rho = \{x \mapsto (L, 1), y \mapsto (L, -1)\}$  and stack distance  $sd = 3$ . Compute  $\text{code}_V \ e \ \rho \ sd$ . Annotate every instruction with the current stack distance like in the examples in the lecture.