

Virtual Machines

Exercise Sheet 4

Deadline: 13 Mai 2008, during lecture, by email, or in room 02.07.041

Exercise 1:

6 Points

Write the following functions in OCaml (without using OCaml library functions with the same names).

a) *filter*, which takes as argument a predicate p and a list l , and returns the list of elements from l for which p is true.

b) *fold_right*, such that

$$\text{fold_right } f \ e \ [x_1, \dots, x_n] = f(x_1, f(x_2, \dots, f(x_n, e)) \dots).$$

c) *mapi*, such that

$$\text{mapi } f \ [x_1, \dots, x_n] = [f(x_1, 1), \dots, f(x_n, n)].$$

For example, for $f(x, i) = x + i$ and $l = [3, 3, 3]$, *mapi* f l should return $[4, 5, 6]$.

Exercise 2:

4+4 Points

a) Give a formal definition of the function *free* such that $\text{free}(e) \subseteq \text{Vars}$ is the set of global variables in e , where Vars is the set of variables used for building expressions.

b) Determine the set of global variables for each of the following expressions.

- `(fn x => x y) (fn y => y)`
- `fn x,y => z (fn z => z (fn x => y))`
- `(fn x,y => x z (y z)) (fn x => y (fn y => y))`
- `((fn x => x) z) + let a = x;
 x = f y;
 y = z
 in x+y+z`

Exercise 3:

6 Points

Consider the expression $e \equiv \text{if } x > 1 \text{ then } x \text{ else } x + y * x$ along with the address environment $\rho = \{x \mapsto (L, 1), y \mapsto (L, -1)\}$ and stack distance $sd = 3$. Compute $\text{code}_V e \ \rho \ sd$. Annotate every instruction with the current stack distance like in the examples in the lecture.