

# Virtual Machines

## Exercise Sheet 8

Deadline: 17 June 2008, during lecture, by email, or in room 02.07.041

### Exercise 1:

10 Points

The following is the straightforward method of computing Fibonacci numbers using a recursive function.

```
letrec fib = fn x => if x <= 1 then 1 else (fib (x-1)) + (fib (x-2))
in fib 4
```

The following example shows how to accomplish the same using a tail-recursive function.

```
letrec fib_aux = fn n, next, result => if n <= 1 then result
                                     else (fib_aux (n-1) next + result, next);
      fib_main = fn n => (fib_aux n 2 1)
in fib_main 4
```

Generate  $code_V$  for this new expression with  $sd = 0$  and  $\rho = \{\}$  using CBV.

### Exercise 2:

6 Points

Write a prolog program including following predicates:

- $last/2$  where the first parameter is a list and the second one is the last element of this list (e.g.  $last([1,2,3],3)$ ).
- $reverse/2$  with two lists as parameters, where one is the reverse list of the other. (e.g.  $reverse([1,2,3],[3,2,1])$ )
- $chain/2$  with two lists, where the first list includes the second one as connected chain. (e.g.  $chain([1,2,3,4,5,6],[2,3,4])$ )

Note: You can write auxiliary predicates if needed.

### Exercise 3:

4 Points

Produce  $code_A/code_G$  for the following terms/goals !

- $f(X, g(b, Y), g(\bar{X}, \bar{Z}))$
- $p(f(g(X, h(\bar{Y}, -), b), Z))$

Use the following address environment:  $\rho = \{X \mapsto 1, Y \mapsto 2, Z \mapsto 3\}$  !