

With **CBN**, we generate for the access to a variable:

$$\text{code}_V x \rho \text{sd} = \text{getvar } x \rho \text{sd} \\ \text{eval}$$

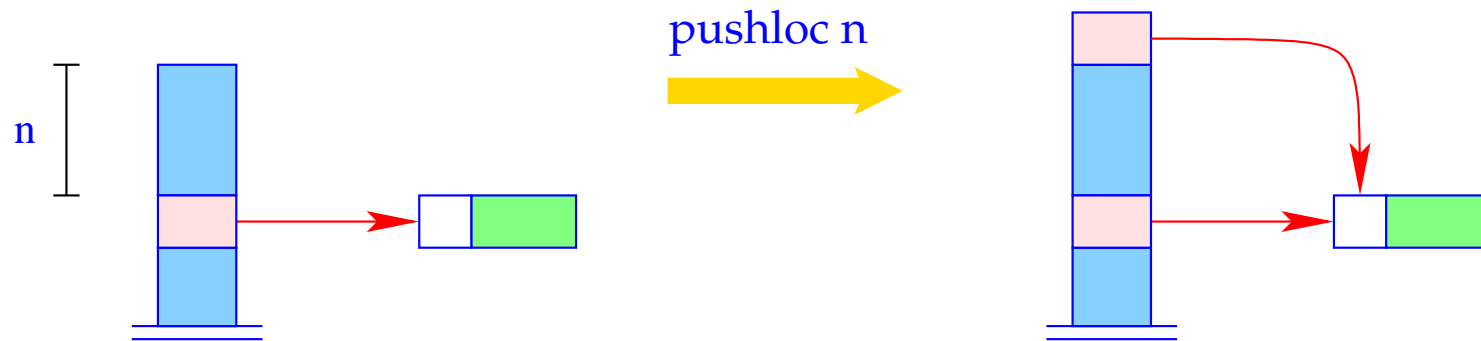
The instruction **eval** checks, whether the value has already been computed or whether its evaluation has to yet to be done (\implies will be treated later :-)

With **CBV**, we can just delete **eval** from the above code schema.

The (compile-time) macro **getvar** is defined by:

$$\text{getvar } x \rho \text{sd} = \text{let } (t, i) = \rho x \text{ in} \\ \text{case } t \text{ of} \\ \quad L \Rightarrow \text{pushloc } (\text{sd} - i) \\ \quad G \Rightarrow \text{pushglob } i \\ \text{end}$$

The access to local variables:



$S[SP+1] = S[SP - n]; SP++;$

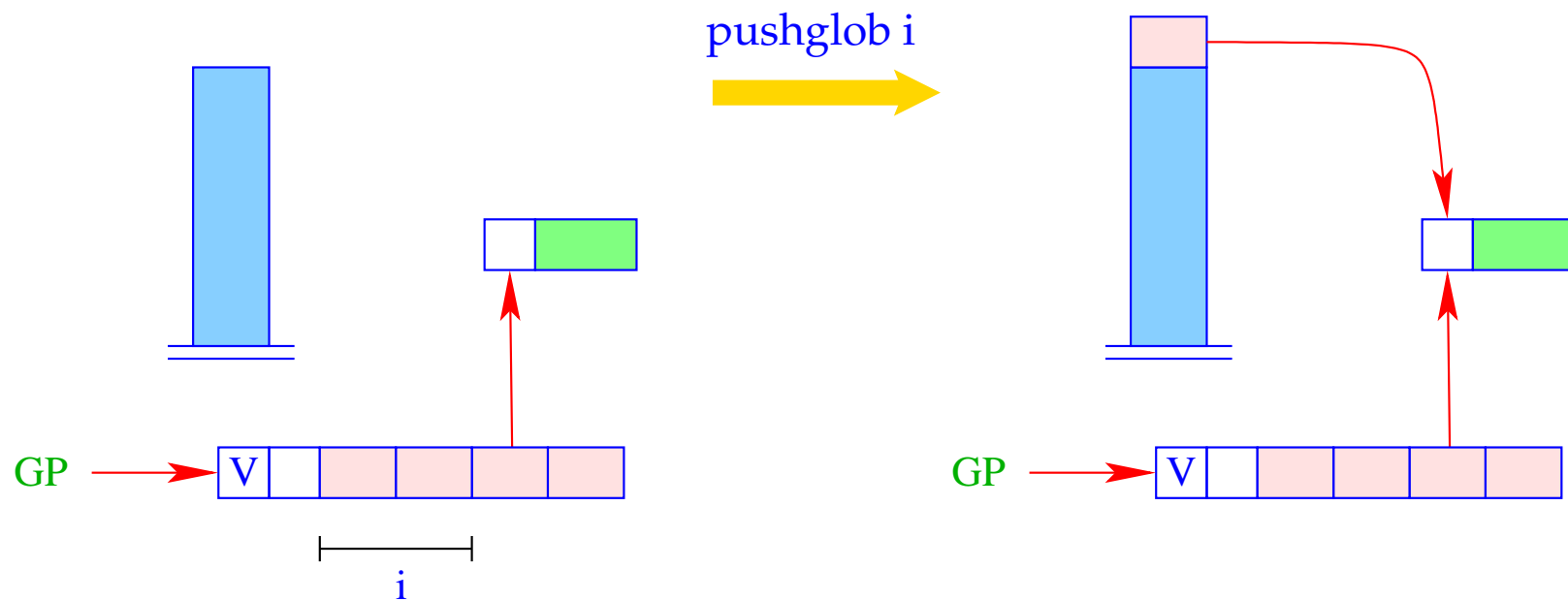
Correctness argument:

Let sp and sd be the values of the stack pointer resp. stack distance **before** the execution of the instruction. The value of the local variable with address i is loaded from $S[a]$ with

$$a = sp - (sd - i) = (sp - sd) + i = sp_0 + i$$

... exactly as it should be :-)

The access to global variables is much simpler:



$SP = SP + 1;$
 $S[SP] = GP \rightarrow v[i];$

Example:

Regard $e \equiv (b + c)$ for $\rho = \{b \mapsto (L, 1), c \mapsto (G, 0)\}$ and $sd = 1$.

With **CBN**, we obtain:

<code>code_v e ρ 1</code>	=	<code>getvar b ρ 1</code>	=	1	<code>pushloc 0</code>
		<code>eval</code>		2	<code>eval</code>
		<code>getbasic</code>		2	<code>getbasic</code>
		<code>getvar c ρ 2</code>		2	<code>pushglob 0</code>
		<code>eval</code>		3	<code>eval</code>
		<code>getbasic</code>		3	<code>getbasic</code>
		<code>add</code>		3	<code>add</code>
		<code>mkbasic</code>		2	<code>mkbasic</code>

15 let-Expressions

As a warm-up let us first consider the treatment of local variables :-)

Let $e \equiv \mathbf{let} \ y_1 = e_1; \dots; y_n = e_n \ \mathbf{in} \ e_0$ be a **let**-expression.

The translation of e must deliver an instruction sequence that

- allocates local variables y_1, \dots, y_n ;
- in the case of
 - CBV**: evaluates e_1, \dots, e_n and binds the y_i to their values;
 - CBN**: constructs closures for the e_1, \dots, e_n and binds the y_i to them;
- evaluates the expression e_0 and returns its value.

Here, we consider the **non-recursive** case only, i.e. where y_j only depends on y_1, \dots, y_{j-1} . We obtain for **CBN**:

```

codeV e ρ sd = codeC e1 ρ sd
                codeC e2 ρ1 (sd + 1)
                ...
                codeC en ρn-1 (sd + n - 1)
                codeV e0 ρn (sd + n)
                slide n // deallocates local variables

```

where $\rho_j = \rho \oplus \{y_i \mapsto (L, \text{sd} + i) \mid i = 1, \dots, j\}$.

In the case of **CBV**, we use `codeV` for the expressions e_1, \dots, e_n .

Warning!

All the e_i must be associated with the same binding for the global variables!

Example:

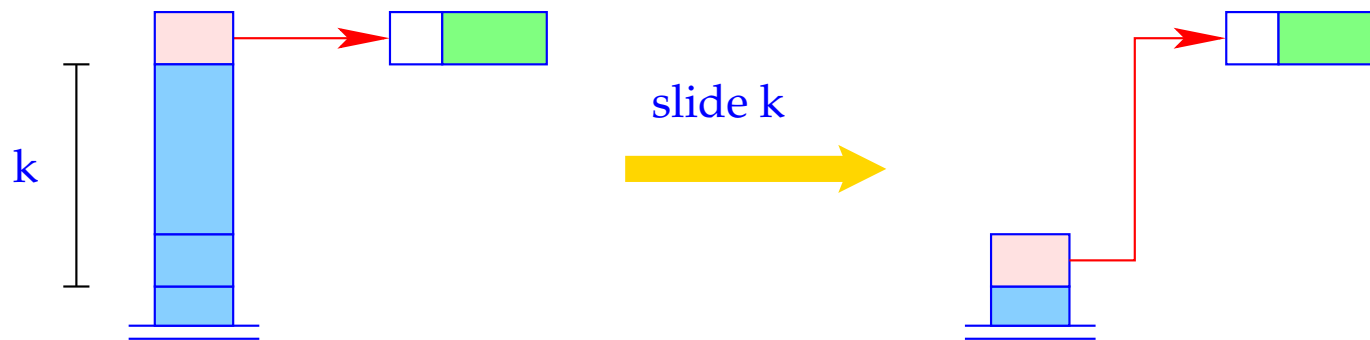
Consider the expression

$$e \equiv \mathbf{let} \ a = 19; b = a * a \ \mathbf{in} \ a + b$$

for $\rho = \emptyset$ and $\mathbf{sd} = 0$. We obtain (for **CBV**):

0	loadc 19	3	getbasic	3	pushloc 1
1	mkbasic	3	mul	4	getbasic
1	pushloc 0	2	mkbasic	4	add
2	getbasic	2	pushloc 1	3	mkbasic
2	pushloc 1	3	getbasic	3	slide 2

The instruction `slide k` deallocates again the space for the locals:



$S[SP-k] = S[SP];$
 $SP = SP - k;$

16 Function Definitions

The definition of a function f requires code that allocates a **functional value** for f in the heap. This happens in the following steps:

- Creation of a Global Vector with the binding of the free variables;
- Creation of an (initially empty) argument vector;
- Creation of an F-Object, containing references to these vectors and the start address of the code for the body;

Separately, code for the body has to be generated.

Thus:

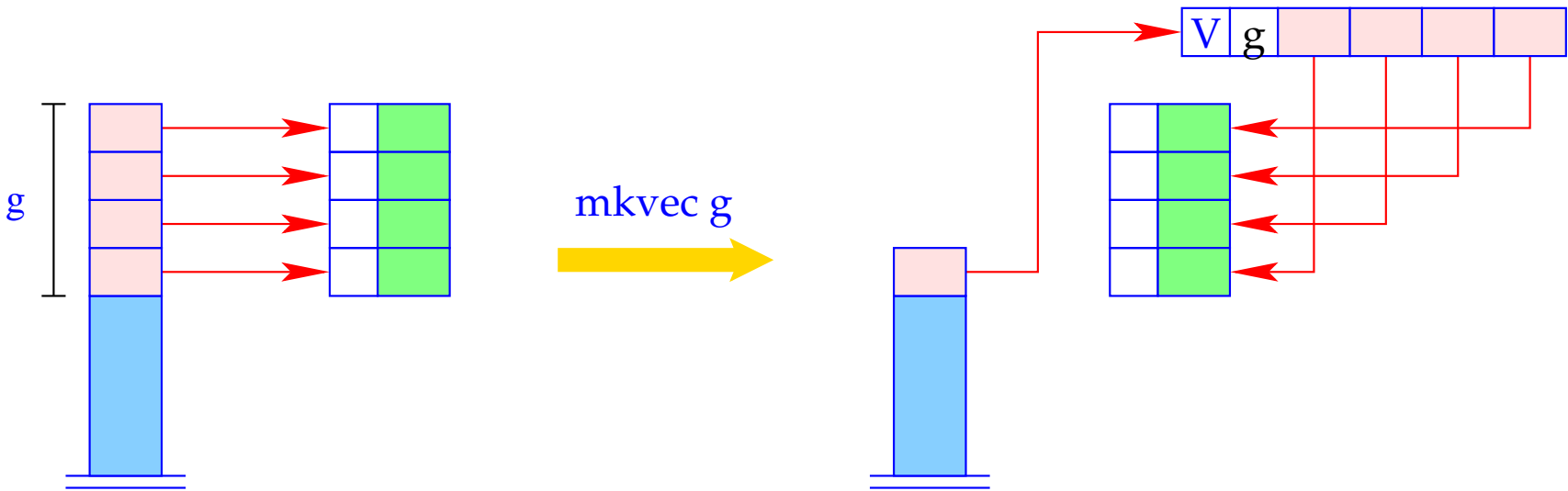
$$\text{code}_V(\mathbf{fn } x_0, \dots, x_{k-1} \Rightarrow e) \rho \text{ sd} =$$

```

getvar z0 ρ sd
getvar z1 ρ (sd + 1)
...
getvar zg-1 ρ (sd + g - 1)
mkvec g
mkfunval A
jump B
A : targ k
    codeV e ρ' 0
    return k
B : ...

```

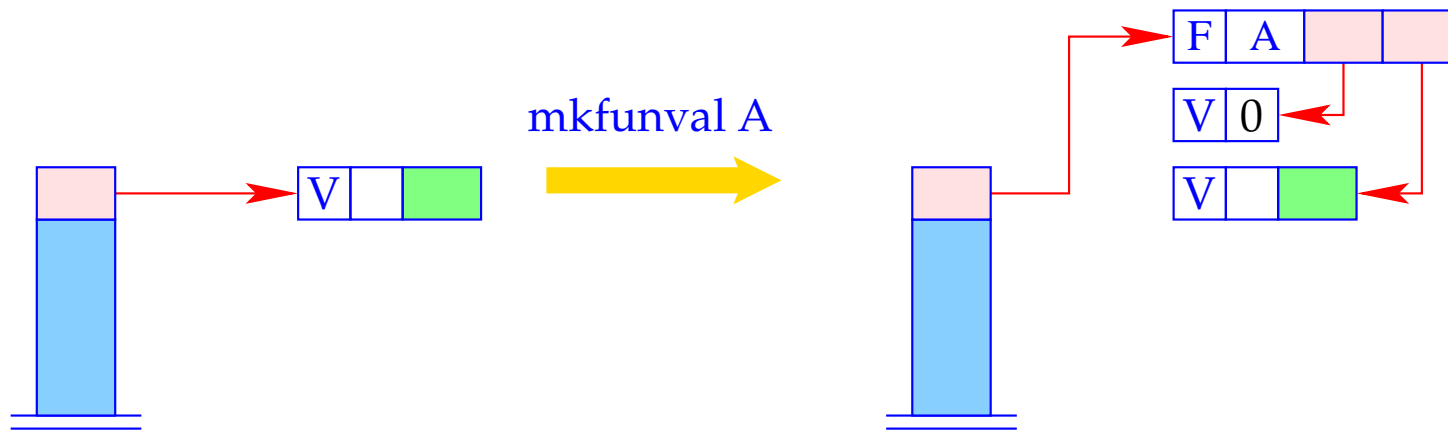
where $\{z_0, \dots, z_{g-1}\} = \text{free}(\mathbf{fn } x_0, \dots, x_{k-1} \Rightarrow e)$
and $\rho' = \{x_i \mapsto (L, -i) \mid i = 0, \dots, k-1\} \cup \{z_j \mapsto (G, j) \mid j = 0, \dots, g-1\}$



```

h = new (V, n);
SP = SP - g + 1;
for (i=0; i<g; i++)
    h->v[i] = S[SP + i];
S[SP] = h;

```



```

a = new (V,0);
S[SP] = new (F, A, a, S[SP]);

```

Example:

Regard $f \equiv \text{fn } b \Rightarrow a + b$ for $\rho = \{a \mapsto (L, 1)\}$ and $\text{sd} = 1$.

$\text{code}_V f \rho 1$ produces:

1	pushloc 0	0	pushglob 0	2	getbasic
2	mkvec 1	1	eval	2	add
2	mkfunval A	1	getbasic	1	mkbasic
2	jump B	1	pushloc 1	1	return 1
0	A: targ 1	2	eval	2	B: ...

The secrets around `targ k` and `return k` will be revealed later :-)

17 Function Application

Function applications correspond to function calls in **C**.

The necessary actions for the evaluation of $e' e_0 \dots e_{m-1}$ are:

- Allocation of a stack frame;
- Transfer of the actual parameters, i.e. with:
 - CBV**: Evaluation of the actual parameters;
 - CBN**: Allocation of closures for the actual parameters;
- Evaluation of the expression e' to an F-object;
- Application of the function.

Thus for **CBN**:

```

codeV (e' e0 ... em-1) ρ sd = mark A // Allocation of the frame
                                codeC em-1 ρ (sd + 3)
                                codeC em-2 ρ (sd + 4)
                                ...
                                codeC e0 ρ (sd + m + 2)
                                codeV e' ρ (sd + m + 3) // Evaluation of e'
                                apply // corresponds to call
                                A: ...

```

To implement **CBV**, we use `codeV` instead of `codeC` for the arguments e_i .

Example: For $(f\ 42)$, $\rho = \{f \mapsto (L, 2)\}$ and $sd = 2$, we obtain with **CBV**:

```

2 mark A           6 mkbasic           7 apply
5 loadc 42         6 pushloc 4         3 A: ...

```


A Slightly Larger Example:

let $a = 17$; $f = \mathbf{fn}$ $b \Rightarrow a + b$ **in** f 42

For **CBV** and $sd = 0$ we obtain:

0	loadc 17	2		jump B	2		getbasic	5		loadc 42
1	mkbasic	0	A:	targ 1	2		add	5		mkbasic
1	pushloc 0	0		pushglob 0	1		mkbasic	6		pushloc 4
2	mkvec 1	1		getbasic	1		return 1	7		apply
2	mkfunval A	1		pushloc 1	2	B:	mark C	3	C:	slide 2