

# Cryptographic Protocols

Winter Semester 2005

1. Homework

25 November 2005

## Exercise 1:

Consider the following modified version of the Needham-Schroeder public key protocol where both nonces  $N_a$  and  $N_b$  are sent in the third message.

1.  $A \longrightarrow B : \{A, N_a\}_{K_b}$
2.  $B \longrightarrow A : \{N_a, N_b\}_{K_a}$
3.  $A \longrightarrow B : \{N_a, N_b\}_{K_b}$

What are the security properties of this protocol ?

## Exercise 2:

Given positive integers  $a, x$  and  $n$ , show that the value  $a^x \bmod n$  can be computed in time polynomial in the total number of bits in the binary representation of the integers.

## Exercise 3:

Define *generalized graphs* to be of the form  $G = (V, E)$  where  $V$  is a set of *vertices* and  $E$  is a set of *edges* of the form  $v_1, \dots, v_n \Rightarrow v_0$  where  $n \geq 0$  and  $v_i$  are vertices. The set of *reachable* vertices in  $G$  is defined inductively by the following rule: if  $v_1, \dots, v_n \Rightarrow v_0$  is an edge in  $E$  and  $v_i$  is reachable for  $1 \leq i \leq n$  then  $v_0$  is reachable. It can be decided in linear time whether a vertex is reachable in such a graph.

Use this to show that the intruder deduction problem can be solved in linear time.